

**TRENTO, 2022/23**  
**ADVANCED GROUP THEORY**  
**EXERCISE SHEET # 11**

*Exercise 11.1.* Show that a direct product of isomorphic simple groups is characteristically simple.

*Exercise 11.2.* Define soluble groups, state and prove the equivalent characterizations, and state and prove the properties with respect to subgroups, quotients and homomorphic images.

*Exercise 11.3.* Prove Burnside's theorem about the solubility of finite groups whose order is divisible by at most two primes, and the results leading to it.