

**TRENTO, 2020/21**  
**ADVANCED GROUP THEORY**  
**EXERCISE SHEET # 11**

*Exercise 11.1.* Show *without* using characters that if  $G$  is a finite group,  $N \trianglelefteq G$  and  $x \in G$ , then

$$|C_G(x)| \geq |C_{G/N}(xN)|.$$

*Exercise 11.2.* State and prove Burnside's formula for the product of the sums of two conjugacy classes.